이산수학

| 개설학기 | 2018학년도 2학기 |  |  |  |  |  |  |
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| 소 속 | 컴퓨터학부 |  |  |  |  |  |  |
| 교 수 명 | 아난드 폴 |  |  |  |  |  |  |
| 학 점 | 3 |  |  |  |  |  |  |
| 수업목표 | The main objective of this course it to give basic outlook on Discrete Mathematics which includes, propositions, Induction, proof patterns, Graph Theory and functions. Some advanced topics shall also be covered |  |  |  |  |  |  |
| 주차 | 주차별 학습내용 | 차시(모듈) | 차시별 학습내용 | 학습목표 | 학습목차 | 학습자료 | PPT 슬라이드 수 |
| 1 | Introduction to Class <br> - Online Lecture <br> Logic of Compound <br> Statement | 1 | Introduction | 1. Main goal of this online course on Discrete <br> Mathematics is to lay foundation for Computer <br> Science courses such as data | 1. Why Discrete Mathematics <br> 2. Course Contents <br> 3. Lair Paradox <br> 4. Grading Policy <br> 5. Course Evaluation | 참고문헌, ppt 교안 | 12 |
|  |  | 2 | Do you speak Math | Science courses such as data <br> 1. Make Sense of problems, and try to solve them <br> 2. Mathematical Reasoning Abstractly and Quantitatively <br> 3. Mpthematical Modeling of logic <br> 2. Boolean propositions | 1. Use of Variables <br> 2. Some Mathematical Statement <br> 3. The Language of Sets <br> 4. Apt-Buildder Notationean logic <br> 2. Boolean propositions |  | 13 |
|  |  | 3 | Logic of Compound statement |  |  |  | 15 |
|  | Proposition/ Boolean Logic Proposition/ De Morgan's Law Proposition/ Logic | 1 | Logic of Compound statement | 1. Loglcan operablors: <br> Conditional 4 <br> 2. Logical operators: $\mathrm{Bi}-$ <br> conditional 1 | 1. Rogloan opriablors: <br> Conditional 4 <br> 2. Logical operators: Bi- <br> conditional 1 | 참고문헌, ppt 교안 | 20 |
| 2 |  | 2 | Logic of Compound statement | 1. Tautology and Contradiction <br> 2. Logical Equivalence | 1. Tautology and Contradiction <br> 2. Logical Equivalence |  | 22 |


|  | Equivalence | 3 | Logic of Compound statement | 1. Ivioaus ronens exampie <br> 2. Modus Ponens <br> 3. Modus Tollens <br> 4. Modus Tollens cont.. | 1. Ivioaus ronens exampie <br> 2. Modus Ponens <br> 3. Modus Tollens <br> 4. Modus Tollens cont.. |  | 23 |
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| 3 | HW on Proposition and Logic of Quantified Statement | 1 | Logics of Quantified Statement | 2. Anatomy of a propositional function | 2. Anatomy of a propositional function | 참고문헌, ppt 교안 | 18 |
|  |  | 2 | Logics of Quantified Statement | 1. A note on quarntinters <br> 2. Binding variables <br> 3. Negating quantifications | 1. A nouté ón quanntiniers <br> 2. Binding variables <br> 3. Negating quantifications |  | 25 |
|  |  | 3 | Rules of Inference | 1. Rulendotinn frem Enalict universal quantifier <br> 2. Rules of inference for the existential muantifier | 1. Truncolatinofrom Enalich <br> universal quantifier <br> 2. Rules of inference for the existential auantifier |  | 15 |
| 4 | More on Quantifiers and In Class Practice of <br> - Induction/ Methods of Proofs | 1 | Number Theory | 1. Wny prime numbers? <br> 2. The divides operator <br> 3. Theorem on the divides operator <br> 4. Prime numbers | 1. Wny prime numbers? <br> 2. The divides operator <br> 3. Theorem on the divides operator <br> 4. Prime numbers | 참고문헌, ppt 교안 | 19 |
|  |  | 2 | Number Theory and Method of Proof | 1. Pseuवorandom numbers <br> 2. The Caesar cipher <br> 3. Rot13 encoding | 1. sseuaorandom numbers <br> 2. The Caesar cipher <br> 3. Rot13 encoding |  | 17 |
|  |  | 3 | Method of Proof | 1. Proof by contradiction <br> 2. A note on that problem... <br> 3. How others explain proof by contradiction | 1. Proof by contradiction <br> 2. A note on that problem... <br> 3. How others explain proof by contradiction |  | 27 |
|  | Induction practice in the class Strong Induction | 1 | Set Part | 1. What is a set? <br> 2. Set properties <br> 3. Specifying a set <br> 4. Often used sets | 1. What is a set? <br> 2. Set properties <br> 3. Specifying a set <br> 4. Often used sets | 참고문헌, ppt 교안 | 21 |
| 5 |  | 2 | Set Part | 1. Proper subsets: Venn diagram <br> 2. Set cardinality | 1. Proper subsets: Venn diagram <br> 2. Set cardinality |  | 32 |


|  |  | 3 | Set Part | 1. Set Iaentities <br> 2. How to prove a set identity <br> 3. What we are going to prove... <br> 1- Dranf heurina bacir cat | I. Set identities <br> 2. How to prove a set identity <br> 3. What we are going to prove... <br> 1- Dronf hewerina hacis cot |  | 31 |
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| 6 | Number Theory with Example and Practice | 1 | Function Part | 1. Definition of a function <br> 2. Function terminology <br> 3. More functions <br> 4. Even more functions | 1. Definition of a function <br> 2. Function terminology <br> 3. More functions <br> 4. Even more functions | 참고문헌, ppt 교안 | 15 |
|  |  | 2 | Inverse Function | 1. More on inverse functions 2. set X mapping into a Set Y | 1. More on inverse functions 2. set $X$ mapping into a Set $Y$ |  | 23 |
|  |  | 3 | Function Part | 1. Graphs of functions <br> 2. Compositions of functions <br> 3. Useful functions <br> 4. Sample floor/ceiling questions | 1. Graphs of functions <br> 2. Compositions of functions <br> 3. Useful functions <br> 4. Sample floor/ceiling questions |  | 20 |
| 7 | Sequence | 1 | Induction I_Sequence | 1. verlintions <br> 2. Sequences <br> 3. Geometric vs. arithmetic sequences | 1. Dellintions <br> 2. Sequences <br> 3. Geometric vs. arithmetic sequences | 참고문헌, ppt 교안 | 30 |
|  |  | 2 | Induction II_Weak and Strong | 1. How do you climb infinite stairs? <br> 2. Let's use that as a proof method | 1. How do you climb infinite stairs? <br> 2. Let's use that as a proof method |  | 28 |
|  |  | 3 | Induction III_Structual and Recursion | 1. Chess and induction <br> 2. Inducting stones <br> 3. Recursion <br> 4. Fibonacci sequence | 1. Chess and induction <br> 2. Inducting stones <br> 3. Recursion <br> 4. Fibonacci sequence |  | 40 |
| 8 |  | 1 | RELATIONS | 2. Representing relations <br> 3. Relations vs. functions | 2. Representing relations <br> 3. Relations vs. functions | 참고문헌, ppt 교안 | 21 |
|  | Sets <br> Function Introduction | 2 | RELATIONS | 2. Combining relations via Boolean operators | 2. Combining relations via Boolean operators |  | 23 |


|  |  | 3 | RELATIONS | 1. Representing relations using directed graphs <br> 2. Reflexivity <br> 3.Irreflexivity | 11. Representing relations using directed graphs <br> 2. Reflexivity <br> 3-Irreflexivity |  | 26 |
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| 9 | and Inverse Function example | 1 | Relations App | 1. 6 degrees of separation <br> 2. Connectivity relation <br> 3. How long are the paths in <br> a transitive closure? | 1. 6 degrees of separation <br> 2. Connectivity relation <br> 3. How long are the paths in a transitive closure? |  | 21 |
|  |  | 2 | RSA Relations App | 1. Private key cryptography <br> 2. Public key cryptography <br> 3. Is that number prime? <br> 4. More on the Fermat <br> pripality tect | 1. Private key cryptography <br> 2. Public key cryptography <br> 3. Is that number prime? <br> 4. More on the Fermat primality tect | 참고문헌, ppt 교안 | 32 |
|  |  | 3 | PGP Relations App | 2. How to "crack" PGP <br> 3. Man-in-the-middle attack: | 2. How to "crack" PGP <br> 3. Man-in-the-middle attack: |  | 21 |
| 10 | Relations and Recurrence | 1 | Counting | 1. The product rule <br> 2. The sum rule <br> 3. More complex counting problems <br> 4. The inclusion-exclusion | 1. The product rule <br> 2. The sum rule <br> 3. More complex counting problems <br> 4. The inclusion-exclusion | 참고문헌, ppt 교안 | 19 |
|  |  | 2 | Permutation and Combination | 1. The pigeonhole principle <br> 2. Generalized pigeonhole principle <br> 3. Sample questions | 1. The pigeonhole principle <br> 2. Generalized pigeonhole principle <br> 3. Sample questions |  | 33 |
|  |  | 3 | Pascal's Triangle | 1. Polynomial expansion <br> 2. Polynomial expansion: The binomial theorem | 1. Polynomial expansion <br> 2. Polynomial expansion: The binomial theorem |  | 27 |
|  |  | 1 | Graph Theory part | 3. Sascal's trianal ot <br> nigsberg <br> 2. A Graph <br> 3. Fuler's Solution | 1. Sevenen briages of Ko nigsberg <br> 2. A Graph <br> 3 Fuler's Salution |  | 17 |
| 11 | Graph Theory Discussion | 2 | Graph Theory part | 2. Graph Isomorphism <br> 3. Are These Isomorphic? | 2. Graph Isomorphism <br> 3. Are These Isomorphic? | 참고문헌, ppt 교안 | 26 |


|  |  | 3 | Graph Theory part | 1. Partitioned into Simple Cycles <br> 2. Proof <br> 3. Tree | 1. Partitioned into Simple Cycles <br> 2. Proof <br> 3. Tree |  | 30 |
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| 12 | More on Graph and Trees its related algorithm | 1 | Application of Graphs | 1. minimum spanning tree <br> 2. Prim's Algorithm <br> 3. Kruskal's Algorithm <br> 4. Adjacency matrix for graph <br> 5. Single Source Shortest Path <br> Algorithm | 1. minimum spanning tree <br> 2. Prim's Algorithm <br> 3. Kruskal's Algorithm <br> 4. Adjacency matrix for graph <br> 5. Single Source Shortest Path <br> Algorithm | 참고문헌, ppt 교안 | 22 |
|  |  | 2 | Algorithm | 1. What is an algorithm? <br> 2. Some algorithms are harder than others <br> 3. Algorithm 1: Maximum element <br> 4. Maximum element running time | 1. What is an algorithm? <br> 2. Some algorithms are harder than others <br> 3. Algorithm 1: Maximum element <br> 4. Maximum element running time |  | 26 |
|  |  | 3 | Algorithm | 1. Insertion sort running time <br> 2. Comparison of running times <br> 3. How does one measure algorithms <br> 4. Bubble sort running time <br> 5-An_acide-ineaualitioc | 1. Insertion sort running time <br> 2. Comparison of running times <br> 3. How does one measure algorithms <br> 4. Bubble sort running time <br> 5_ An_acide-inecualitioc |  | 32 |
|  |  | 1 | Review of DM | 1. Logics <br> 2. Application: A More Complex Deduction <br> 3. Proof <br> 4. Tarski's World <br> timonacct | 1. Logics <br> 2. Application: A More Complex Deduction <br> 3. Proof <br> 4. Tarski's World |  | 19 |
| 13 | Probability and Counting | 2 | Review of DM | 2. Mathematical Induction Works Using Dominoes <br> 3 Ruccall'c Parador | 2. Mathematical Induction <br> Works Using Dominoes <br> 3 Ruccall's Paradov | 참고문헌, <br> not 규아 | 15 |


|  |  | 3 | Finite State Machine | 1. Introduction <br> 2. Machine <br> 3. Finite-State Machine <br> 4. Diagraph Notation <br> 5. Newspaper Vending Box Digraph <br> 6. Reqular Expressions | 1. Introduction <br> 2. Machine <br> 3. Finite-State Machine <br> 4. Diagraph Notation <br> 5. Newspaper Vending Box Digraph <br> 6. Reqular Expressions | - - - | 17 |
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