

Course webpage

[https://docs.google.com/document/d/1VgiEzjb6AMoFThTljSAPLWwEbrBW\\_qAhjtStF5t-LQ/edit?usp=sharing](https://docs.google.com/document/d/1VgiEzjb6AMoFThTljSAPLWwEbrBW_qAhjtStF5t-LQ/edit?usp=sharing)

BUS403

예습 및 선행학습 불필요. 쓸데없이 시간 낭비 하지 마세요.

중학교 수준의 수학으로도 충분합니다. 수학보다 직관과 상상력이 중요합니다.

재무에 관한 사전지식 전혀 필요 없습니다.

중요한 사항은 한국어로 복습합니다.

리포트 토픽은 본인이 제안할 수도 있고 교수로부터 받을 수도 있습니다.

학점은 절대평가 입니다.

Only term paper will determine your grade. There won't be any exam at all.

No prior knowledge on finance or mathematics is required.

The class topics can be changed on the request of students.

Textbooks and materials

- <https://class.coursera.org/fe1-001/lecture>
- <https://class.coursera.org/fe2-001/lecture>
- [Fixed Income Securities: Valuation, Risk, and Risk Management](#), Pietro Veronesi (University of Chicago, Booth School of Business), January 2010, ©2011 ([slides](#))
- (sub) 자본시장법

## **Weeks and schedule (very preliminary. will be updated shortly)**

1. Class introduction (Martingale 1)

Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))

2. Thanksgiving day
3. Martingale 2

Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))

[Cronqvist, H., & Siegel, S. \(2014\). The genetics of investment biases. Journal of Financial Economics, 113\(2\), 215-234.](#)

4. Veronesi ch02 (2.1-2.3); Continuous time some basics ([link](#); very good, but many errata)

[http://en.wikipedia.org/wiki/Flipped\\_classroom](http://en.wikipedia.org/wiki/Flipped_classroom)

Student presentation: Veronesi ch02 (2.1-2.3; pp29-43) 김민령  
Bring one page proposal for your term paper by next class  
Listen week 1 at <https://class.coursera.org/fe1-001/lecture>  
Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))

5. Sigma algebra, measure, information structure  
Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))  
Discussion week 1 at <https://class.coursera.org/fe1-001/lecture>  
HW: Listen week 2 at <https://class.coursera.org/fe1-001/lecture>

6. Veronesi ch02 (2.4-2.5; 조연정); Veronesi ch02 (2.8; 이태훈)  
Listen week 2 at <https://class.coursera.org/fe1-001/lecture>  
Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))  
HW: Listen week 2 (2.6-2.7) at <https://class.coursera.org/fe1-001/lecture>

7. Veronesi ch03 (3.2; Felix)  
Binomial option pricing model: replicating portfolio  
Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))  
HW: Listen week 3 (3.1-3.4) at <https://class.coursera.org/fe1-001/lecture>

8. 0926 Veronesi ch03 (3.3-3.4; Niklas)  
Binomial option pricing model: risk neutral valuation  
Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))  
HW: Listen week 3 (3.5-3.8) at <https://class.coursera.org/fe1-001/lecture>

9. 1001 Veronesi ch03 (3.7; 유정빈)  
Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))  
HW: Listen week 4 (4.1-4.3) at <https://class.coursera.org/fe1-001/lecture>  
[Mathematical constant](#); [natural logarithm](#)  
Multi step binomial tree ([wikipedia](#))  
Bring your laptop

10. 1003 National Foundation Day

11. Multi step binomial tree ([wikipedia](#)); [Binomial Model \(option and futures\)](#)  
HW: Listen week 4 (4.5-4.8) at <https://class.coursera.org/fe1-001/lecture>  
[Mathematical constant](#); [natural logarithm](#)

12. 1010 Veronesi ch04 (4.1; 조연정)  
Ou-Yang Hui and Hua He's note ([note1](#), [note2](#))  
[Binomial Model \(option and futures\)](#): Dividend  
[Binomial tree example](#) for interest rate derivatives  
HW: Listen week 5 (5.1-5.4) at <https://class.coursera.org/fe1-001/lecture>

13. 1015 Veronesi ch05 (5.1-5.2; 김민령)

[Excel VBA](#)

[Binomial Model \(option and futures\)](#): Dividend

[Binomial tree example](#) for interest rate derivatives

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Inputs

- $\sigma$ : Volatility
- S: Current stock price
- K: Strike price
- T: Time to maturity (years)
- r: Risk free rate
- q: Dividend rate (per year)

Outputs ([Excel Example](#))

- $c = e^{-rT} [FN(d_1) - KN(d_2)]$ : price of European call option
  - $p = e^{-rT} [KN(-d_2) - FN(-d_1)]$ : price of European put option
  - $$d_1 = \frac{\ln(F/K) + (\sigma^2/2)T}{\sigma\sqrt{T}}$$
  - $$d_2 = \frac{\ln(F/K) - (\sigma^2/2)T}{\sigma\sqrt{T}} = d_1 - \sigma\sqrt{T},$$
  - $F = Se^{(r-q)T}$ .
- 

[VBA for Black Scholes Model](#)

14. 1017 Veronesi ch05 (5.3-5.4; 이태훈)

Excel VBA Practice for [Binomial Model \(option and futures\)](#)

[VBA for binomial tree model](#)

15. 1022 Veronesi ch06 (6.1; Niklas)

Forward Price and Futures Price

Generating random variables: rand(), randbetween(a, b), normsinv(rand()),...

Brownian Motion

Geometric Brownian Motion and Stock Prices

16. 1024 Veronesi ch06 (6.2; Felix)

Arrow Debreu Securities @[Binomial Model \(option and futures\)](#)

17. 1029 Arrow Debreu Securities @[Binomial Model \(option and futures\)](#)

Generating random variables: rand(), randbetween(a, b), normsinv(rand()),...

Brownian Motion

Geometric Brownian Motion and Stock Prices

18. 1031 Veronesi ch08 (8.1-8.2 김민령)

Simulating stock price

[Computing VaR](#): We will conduct a 1-day and 10-day VaR (95%, 99%) analysis using the Monte Carlo simulation method. Let us simply assume that 10-day VaR is simply  $10^{0.5}$  times the 1-day VaR.

Definition 1: Given a confidence level  $\alpha$  in  $(0,1)$ , the Value-at-Risk of a portfolio at  $\alpha$  over the time period  $t$  is given by the smallest real number  $k$  such that the probability of a loss over a time interval  $t$  greater than  $k$  is  $\alpha$ .

Example: Suppose a hypothetical bond portfolio has a “one-day VaR at a confidence level of 5% of \$10 million.” This means that over a typical one-day period, the bond portfolio will lose \$10 million or more only 5% of the time.

19. 1105 Homework day

20. 1107 한양대학교 전체교수회의

21. 1112 Veronesi ch08 (8.3 조연정)

Simulating stocks and derivatives prices in risk neutral world

[VBA simulation and option pricing](#)

22. 1114 Example 8.2 (p.298; Niklas)

[Pass-through securities](#)

23. 1119 [Simulating correlated random variables \(Cholesky decomposition with VBA\)](#)

24. 1121 Example 8.3 and Effective Duration (p.301) (조연정)

[Simulating correlated random variables \(Cholesky decomposition with VBA\)](#)

```
Sub multiasset()  
  rf = 0.01 'risk free rate  
  T = 2 ' time to maturity (year)  
  v1 = 0.3 'volatility of 1st asset  
  v2 = 0.2 'volatility of 2nd asset  
  rho = 0.1 'correlation between two assets  
  simn = 10 ^ 5 ' # of simulation
```

```

sumv = 0
For i = 1 To simn
    u0 = WorksheetFunction.NormSInv(Rnd)
    u1 = WorksheetFunction.NormSInv(Rnd)
    u2 = rho * u1 + (1 - rho ^ 2) ^ 0.5 * u0
    'u1 and u2 are correlated with rho
    ret1 = (rf - v1 ^ 2 / 2) * T + v1 * T ^ 0.5 * u1
    ret2 = (rf - v2 ^ 2 / 2) * T + v2 * T ^ 0.5 * u2
    gret1 = Exp(ret1) 'gross return from asset 1 by investing in 1 dollar
    gret2 = Exp(ret2)
    optionv = max(gret1, gret2, 0.9)
    sumv = sumv + optionv
Next i
optionv_final = Exp(-rf * T) * (sumv / simn)
Cells(1, 1) = optionv_final
End Sub

Function max(a, b, c)
    If a > b And a > c Then
        max = a
    ElseIf b > a And b > c Then
        max = b
    Else
        max = c
    End If
End Function

```

## Brownian Motion

### Geometric Brownian Motion and Stock Prices

#### [Convertible bond](#)

#### 25. 1126 Example 8.4 (김민령)

Check [this term paper format](#) (DUE 03 DEC)

[Simplico](#); [Real option note](#)

**“DUE DATE FOR TERM PAPER” 20141209 09:00 (submit your term paper to**

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**Final Due Date: 20141220 09:00 (submit your term paper to**

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- \* Please use APA format for your references. See the following example.
- \* Kang, H. G., Joo, H. H., & Cho, J. (2014). Brand-size complementarity in the choice of retail stores. *Applied Economics Letters*, 21(6), 413-416.
- \* The other part of your paper should follow the guideline below.
- \* <http://aom.org/publications/amj/styleguide/>
- \* If you cite a paper in the body of the text like (Kang, Joo and Cho, 2014), this should be specified in the reference list at the end of the paper.
- \* If an article is in the reference list, it should be mentioned at least once in the main body.
- \* [Sample](#) and [further guideline](#)
- \* If you do not follow this format guideline correctly, your grade will be downgraded by two.
- \* [this term paper format](#)

26. 1128 Example 8.5 + TBA Market (Felix)

[Simplico](#)

[Real option note](#)

Computing Implied Volatility

NOTE: Optimization and solver using VBA

```
Sub solverexample()  
SolverReset  
SolverOptions precision:=0.0001  
SolverOk SetCell:=Cells(9, 2), MaxMinVal:=2, _  
    ByChange:="B6:B7", Engine:=2, EngineDesc:="GRG Nonlinear"  
SolverAdd cellRef:=Range("B6"), relation:=3, formulatext:=5  
SolverAdd cellRef:=Range("B7"), relation:=1, formulatext:=5  
SolverSolve userfinish:=False  
End Sub  
  
'SolverAdd cellRef:=Range("G26"), relation:=3, formulatext:=0.01479165  
'SolverAdd cellRef:=Range("B6:B7")
```

27. 1203 Veronesi ch08 (8.4 이태훈)

[Black Scholes Formula Excel Illustration](#)

Computing Implied Volatility

VBA function for Black-Scholes Formula

28. 1205 [Estimating volatilities](#): GARCH(1,1), etc.  
[https://www.dropbox.com/s/qqtfnfv8cmzlf6v/garch\\_FF.xlsm](https://www.dropbox.com/s/qqtfnfv8cmzlf6v/garch_FF.xlsm). Maximum Likelihood Estimation (MLE1; MLE2 (stern); MLE3)
29. 1210 [Estimating volatilities](#): EGARCH(1,1) and GJR-GARCH(1,1), etc.  
[https://www.dropbox.com/s/qqtfnfv8cmzlf6v/garch\\_FF.xlsm](https://www.dropbox.com/s/qqtfnfv8cmzlf6v/garch_FF.xlsm). Maximum Likelihood Estimation (MLE1; MLE2 (stern); MLE3)
30. 1212 [Estimating volatilities](#): EGARCH(1,1) and GJR-GARCH(1,1), etc.  
[https://www.dropbox.com/s/qqtfnfv8cmzlf6v/garch\\_FF.xlsm](https://www.dropbox.com/s/qqtfnfv8cmzlf6v/garch_FF.xlsm). Maximum Likelihood Estimation (MLE1; MLE2 (stern); MLE3) Kang, Hyoung Goo and Kim, Y. Han (Andy) and Lee, Jong Kyu, Can Big Data Predict the Behavior of North Korea? (September 3, 2014). Available at SSRN: <http://ssrn.com/abstract=2490693> or <http://dx.doi.org/10.2139/ssrn.2490693> (NK Slides).
31. Fama-MacBeth regression: Fama, Eugene F.; MacBeth, James D. (1973). "Risk, Return, and Equilibrium: Empirical Tests". [Journal of Political Economy](#) 81 (3): 607–636. [JSTOR 1831028](#). [Booth and Fama \(1992\)](#)
32. Fama-MacBeth regression: Fama, Eugene F.; MacBeth, James D. (1973). "Risk, Return, and Equilibrium: Empirical Tests". [Journal of Political Economy](#) 81 (3): 607–636. [JSTOR 1831028](#).
33. [Kyle Model](#)
34. [Fama-French \(2012\)](#)

## References

- [Merton continuous time finance](#)
- [Jean-Pierre Danthine's intuitive continuous time finance](#)
- Continuous time some basics ([link](#); very good, but many errata)
- Kim SH, Kang H. 2014. [A New Strategy using Term-structure Dynamics of Commodity Futures](#). [Financial Research Letters](#).
- [Piazzesi Affine Term structure models](#)
- [Cox, Ross and Rubinstein 1979](#)
- [http://www.ems.bbk.ac.uk/for\\_students/msc\\_finEng/math\\_methods/](http://www.ems.bbk.ac.uk/for_students/msc_finEng/math_methods/)

## Forthcoming

- \* [Chap14: Interest rate models in continuous time](#)
- \* [Chap15: NO ARBITRAGE AND THE PRICING OF INTEREST RATE SECURITIES](#)
- \* [Ch27](#) Martingale measures ([BSM formula](#))
- \* [Ch28](#) Interest rate derivatives: standard market models
- \* [Chap17: RISK NEUTRAL PRICING AND MONTE CARLO SIMULATIONS](#)
- \* [Chap19: NO ARBITRAGE MODELS AND STANDARD DERIVATIVES](#)
- \* [Chap11: RISK NEUTRAL TREES AND DERIVATIVE PRICING \(excel\)](#)

- [Ch09: One Step Binomial Trees \(excel\)](#)
- [Ch10: Multi-Step Binomial Trees](#)

\* [Chap19: NO ARBITRAGE MODELS AND STANDARD DERIVATIVES](#)

#### Papers

- Bansal, Harvey and Dahlquist ([2004](#); <http://ssrn.com/abstract=594845>)
- Hansen and Richard ([1987 Econometrica](#))
- [Disclosure and agency conflict: Evidence from mutual fund commission bundling](#), Roger M. Edelen, Richard B. Evans, Gregory B. Kadlec, [Journal of Financial Economics](#), Volume 103, Issue 2, February 2012, Pages 308–326
- Fama-MacBeth regression: Fama, Eugene F.; MacBeth, James D. (1973). "Risk, Return, and Equilibrium: Empirical Tests". [Journal of Political Economy](#) 81 (3): 607–636. [JSTOR 1831028](#).
- [Booth and Fama \(1992\)](#)
- [Kyle Model](#)
- [Fama-French \(2012\)](#)
- [Scientific Background on the Sveriges Riksbank Prize in Economic Sciences in Memory of Alfred Nobel 2013](#)

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Actuarial Science: [www.utstat.utoronto.ca/sjaimung/courses/sta2502/main.htm](http://www.utstat.utoronto.ca/sjaimung/courses/sta2502/main.htm)

Continuous time some basics ([link](#); very good, but many errata)

R and efficient frontier: <http://www.calculatinginvestor.com/2011/06/07/efficient-frontier-1/>  
<http://www.idsc.ethz.ch/Courses/stochasticsystem>

Stopping time <http://www.columbia.edu/~ks20/stochastic-I/stochastic-I-ST.pdf>

[Optional stopping theorem](#):

<http://www.columbia.edu/~ks20/>